1.

(a) Compute the price of a European call option written on a non-dividend-paying stock. The current stock price is $100 and the volatility of the stock price is 20%. The maturity of the option is in six months and the strike price is $100.

The risk free interest rate with continuous compounding is 3% per annum. You should use a three period binomial model to price the option.

Also compute the replicating portfolio.

(b) The same as exercise 1a except you should price an American call option.

(c) Again, same as exercise 1a except this time you should price an American put option.

2.

(a) Same as exercise 1b except now the underlying stock will pay a dividend of 5% of the stock value in four months time. Note that you do not have to compute the replicating portfolio for this exercise.

(b) Again, same as exercise 1b except now the underlying stock will pay a dividend

of $5 in four months time. Note that you do not have to compute the replicating portfolio for this exercise.

Note

that you are supposed to price an American call option which means that if early exercise is optimal, it will be so just before dividend payment. Make sure that you use the right stock price! (For American put options early exercise will always be optimal just after dividend payment, so that is why we have not had to think about it.)

3. A stock is expected to pay a dividend of 5% of its value in two months and in four months. The stock price is $100, and the risk-free rate of interest is 3% per annum with continuous compounding. An investor has just taken a long position in a six-month forward contract on the stock.

(a) What are the forward price and the initial value of the forward contract?

(b) Three months later the price of the stock $95 is and the risk-free rate of interest is still 3% per annum. What are the forward price of a six-month forward contract on the stock contracted now, and the value of the long position in the forward contract contracted three months ago?

4. Compute the price of an American call option written on a futures contract. The strike price of the option and the current futures price are both $100 and the time to maturity of the option is six months. The risk free interest rate with continuous compounding is 3% and the volatility of the futures price is 20%. As before, you should use a three period binomial model to price the option.